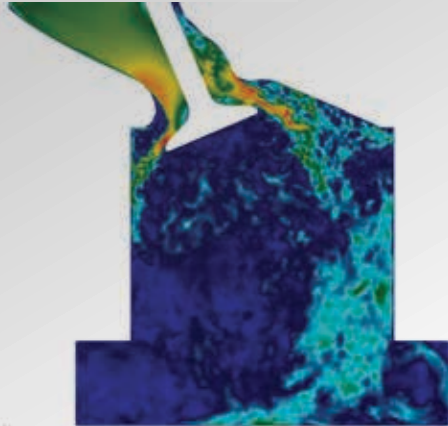


Sensitized-RANS simulations of complex flows in conjunction with ANSA: towards increasing efficiency

Louis Krüger, M. Bopp, S. Jakirlic
Technical University of Darmstadt, Germany



Research Association of Automotive Technology (FAT)

FKFS wind tunnel

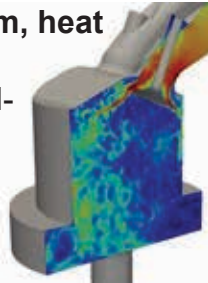


Numerical simulation



German Research Foundation (DFG)

→ Development of a modeling basis for the computational capturing of the simultaneous turbulent momentum, heat and mass transfer processes of developing free shear as well as wall-boundary layers.



→ **Dynamic movement of the rim geometry**

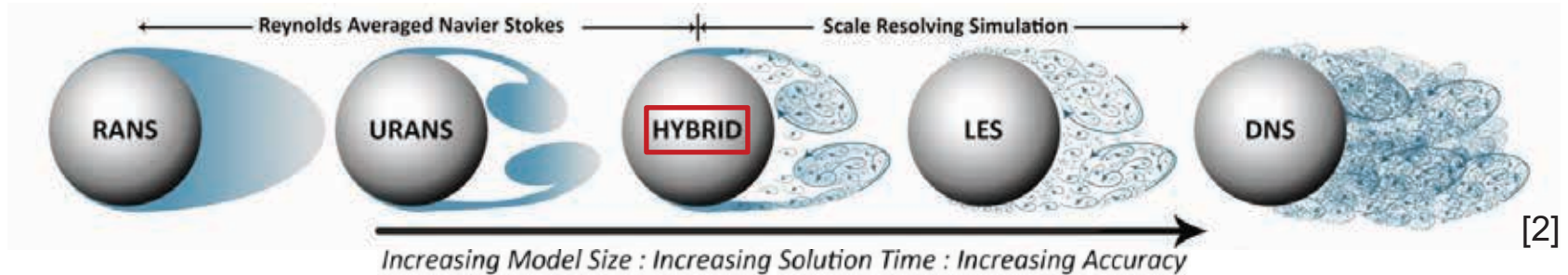
- Transient phenomena due to rim rotation

→ **Hybrid RANS/LES turbulence models**

- Flow fields including turbulent fluctuations

High requirements for the mesh quality → ANSA

On turbulent flow modelling



Navier-Stokes-Equations (NSE)

$$\frac{\partial \bar{U}_i}{\partial x_i} = 0$$

$$\frac{\partial \bar{U}_i}{\partial t} + \bar{U}_j \frac{\partial \bar{U}_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial \bar{p}}{\partial x_i} + \frac{\partial}{\partial x_j} \left(\nu \frac{\partial \bar{U}_i}{\partial x_j} - \underbrace{\bar{u}_i \bar{u}_j}_{\text{RST}} \right)$$

ensemble-averaged, incompressible, Newtonian fluids

RANS/URANS

$k - \omega - \zeta - f$ model
 $k - \omega - \text{SST}$ model
 HJRSM model

HYBRID

ER- $\zeta - f$ model
 DDES - SA model
IIS - RSM model

Computational framework

Eddy-resolving $k - \omega - \zeta - f$ model | IIS-RSM model

$k - \omega - \zeta - f$ model

$$\left(\frac{D\omega}{Dt}\right)_{k-\omega-\zeta-f} + P_{SAS} = \left(\frac{D\omega}{Dt}\right)_{ER-\zeta-f}$$

ER- $\zeta - f$ model

- Four equation (k, ω, ζ, f) near-wall model
- $\zeta = \frac{\overline{v^2}}{k}$ representing a measure for the wall-normal turbulent intensity
- Elliptic function f
 - → no damping functions (to account for the near-wall effects) required

- Introduction of an additional source term motivated by the scale-adaptive simulation (SAS) concept of Menter and Egorov (2010; $k - \omega$ SST SAS)
- Source term formulation proposed by Maduta *et al.* (2015) for a scale-supplying equation based on the specific dissipation rate $\omega = \varepsilon/k$

Goal: enable the model to resolve turbulent fluctuations by suppressing modeled turbulent kinetic energy

Computational framework

Eddy-resolving $k - \omega - \zeta - f$ model | IIS-RSM model

$k - \omega - \zeta - f$ model

$$\left(\frac{D\omega}{Dt}\right)_{k-\omega-\zeta-f} + P_{SAS} = \left(\frac{D\omega}{Dt}\right)_{ER-\zeta-f}$$

ER- $\zeta - f$ model

$$\left(\frac{D\omega}{Dt}\right)_{ER-\zeta-f} = C_{\omega 1} \frac{\omega}{k} P_k - C_{\omega 2} \omega^2 + \frac{\partial}{\partial x_i} \left[\left(\nu + \frac{\nu_t}{\sigma} \right) \frac{\partial \omega}{\partial x_i} \right] + CD + \boxed{P_{SAS}}$$

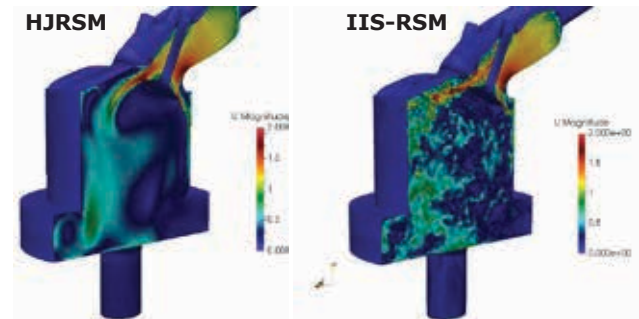
$\xrightarrow{\quad} P_{SAS} = f(\nabla^2 U_i)$

HJRSM model

$$\left(\frac{D\omega^h}{Dt}\right)_{HJRSM} + P_{SAS} = \left(\frac{D\omega^h}{Dt}\right)_{IIS-RSM}$$

IIS-RSM model

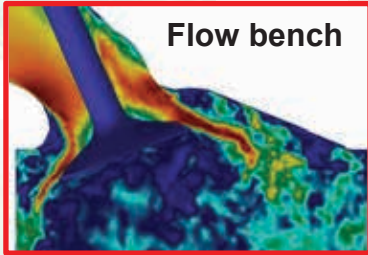
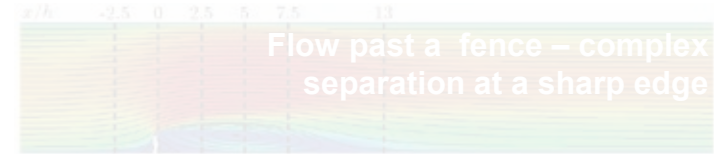
The model doesn't explicitly include a grid-dependent parameter:
⇒ towards a grid-spacing-free model formulation



Predictive performances

Tandem cylinder
(different in-between distances)

Physiological flow in
an aortic aneurysm



2D hill

Plungin

$VT = 0.30$

ction

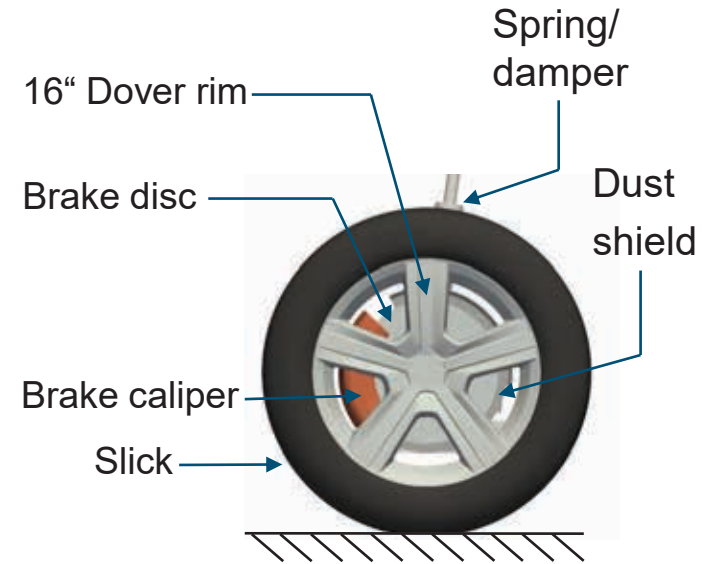
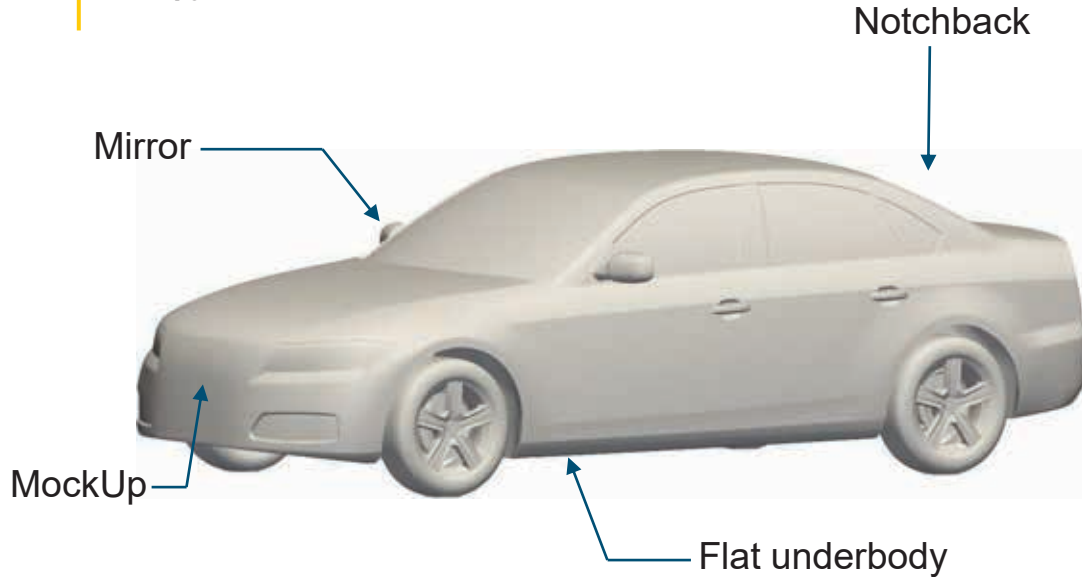
(with plasma-actuated flow control)

Impinging jet (heat transfer)

Car configuration: DrivAer

A. Heft (2014)

100% model



$4.61 \times 2.03 \times 1.42 \text{ m (L} \times \text{W} \times \text{H)}$

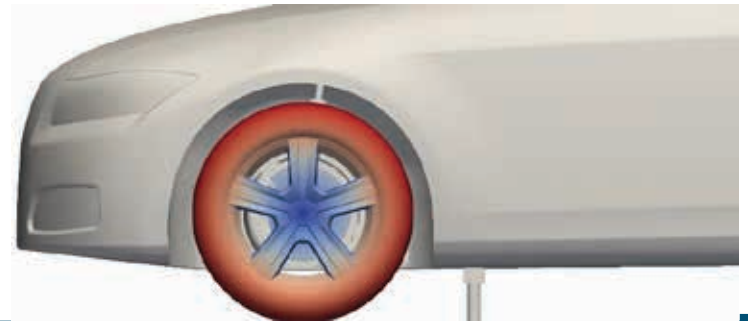
Wheel rotation approach

Tangential velocity

Multiple Reference Frame

Sliding Mesh

- Stationary approximation
- Rim rotation using velocity boundary condition
- Specify rotational axis + angular velocity



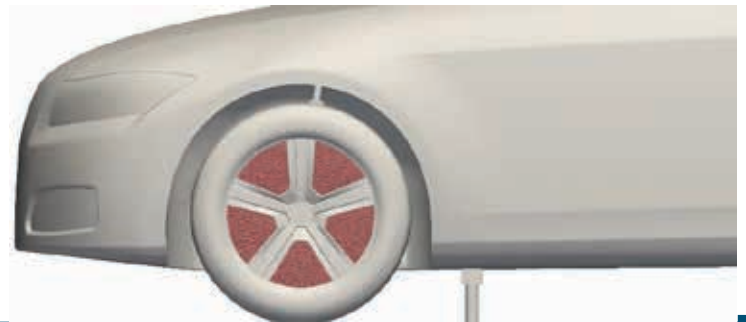
Wheel rotation approach

Tangential velocity

Multiple Reference Frame

Sliding Mesh

- Stationary approximation
- Moving reference coordinate system
- Mesh regions: inertial system and reference system (MRF region)
- Additional apparent forces: Coriolis and centrifugal force



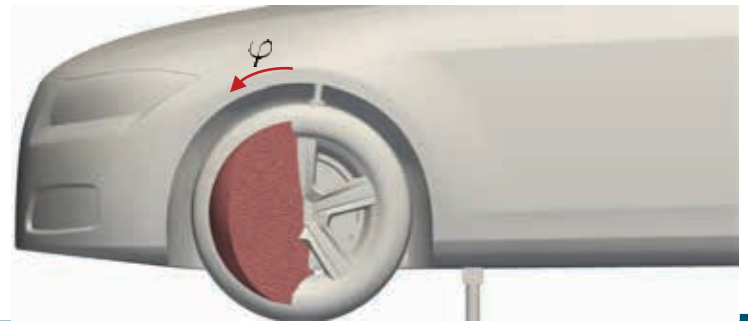
Wheel rotation approach

Tangential velocity

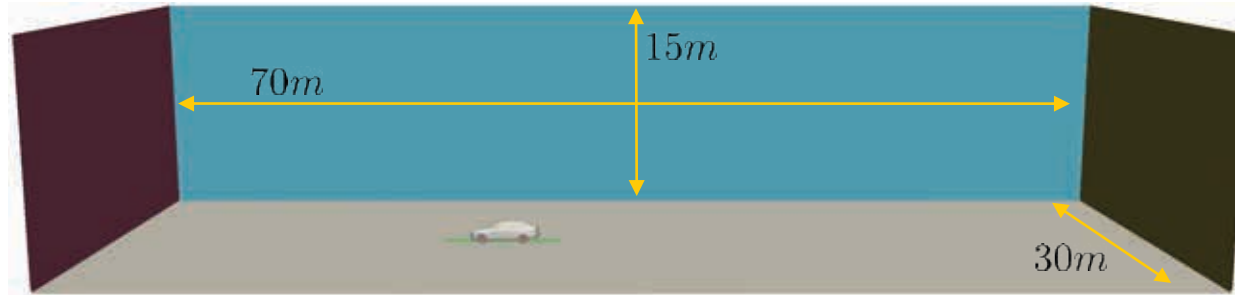
Multiple Reference Frame

Sliding Mesh

- Unsteady approach
- Dynamic rotation of the rim geometry
- Steady and unsteady mesh regions
- 0.5 degrees rim rotation/time step



Computational domain & boundary conditions



- Inlet velocity: $U_b = 140 \text{ km/h}$
- Full moving ground approach
- ~ 46 Mio. volume cells, $y^+ < 5$
- 28 simulations, OpenFOAM
- CPU hours > 15 Mio.



Global flow topology

ER- ζ - f model, $y = 0\text{m}$

instantaneous

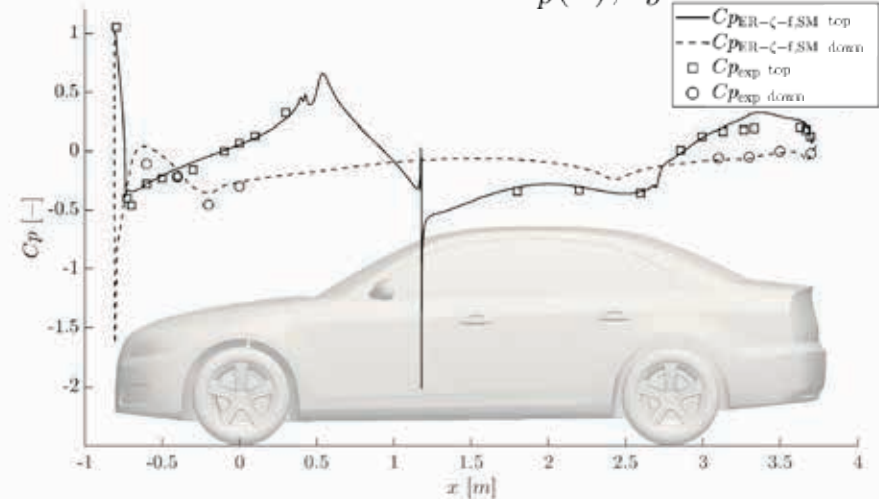


averaged



0.0 U/U_b 1.7

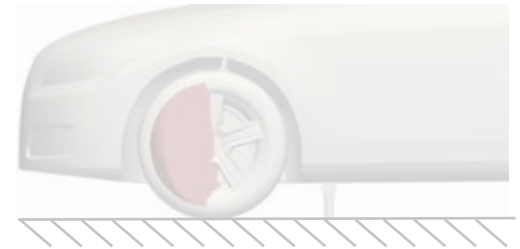
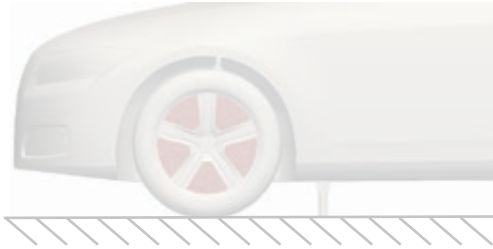
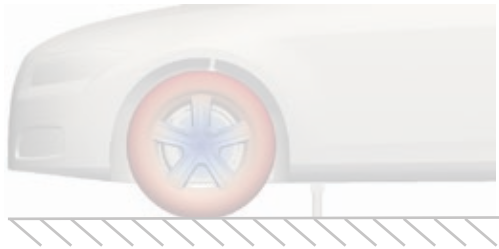
Pressure coefficient $C_p(x)$, $y = 0\text{m}$



$$C_p(x) = \frac{p_x - p_\infty}{\frac{1}{2} \rho_L U_b^2}$$

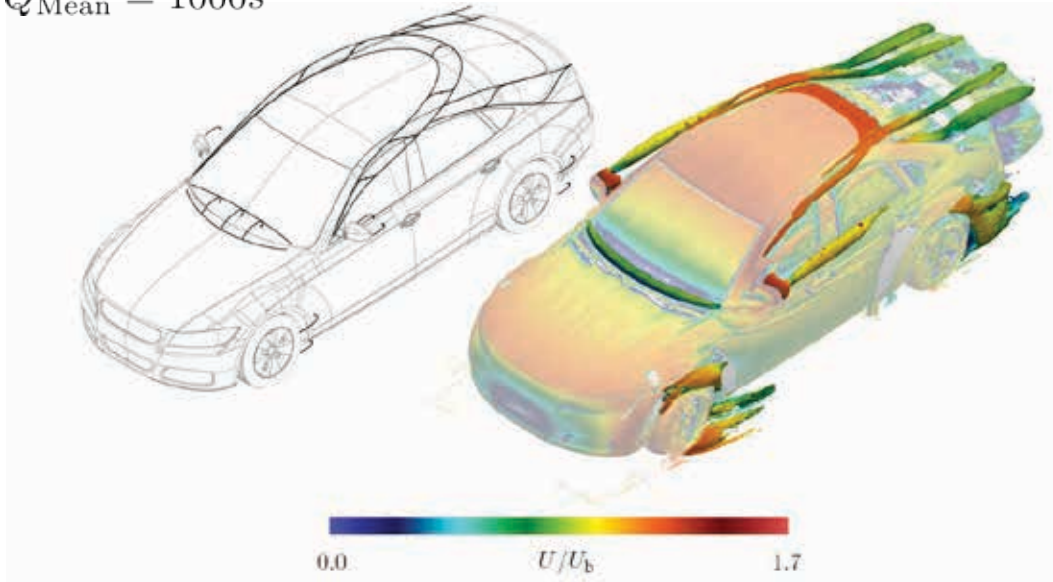
1. What is the impact of the wheel rotation approach?
2. What is the influence of the turbulence model?

What is the impact of the wheel rotation approach?



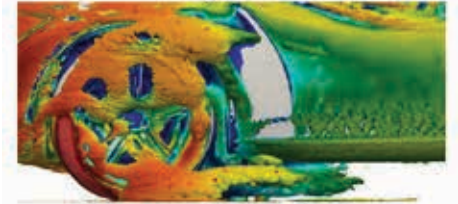
Characteristic vortex structures

$$Q_{\text{Mean}} = 1000s^{-1}$$

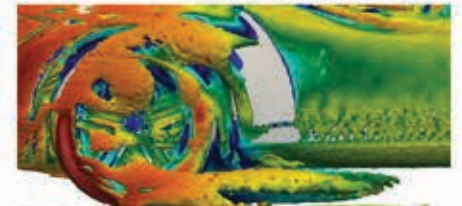


$$Q_{\text{Mean}} = 1/2 \left(\|\bar{\Omega}_{ij}\|^2 - \|\bar{S}_{ij}\|^2 \right)$$

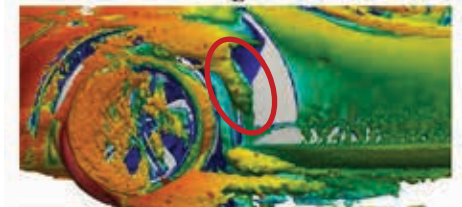
TangVelo



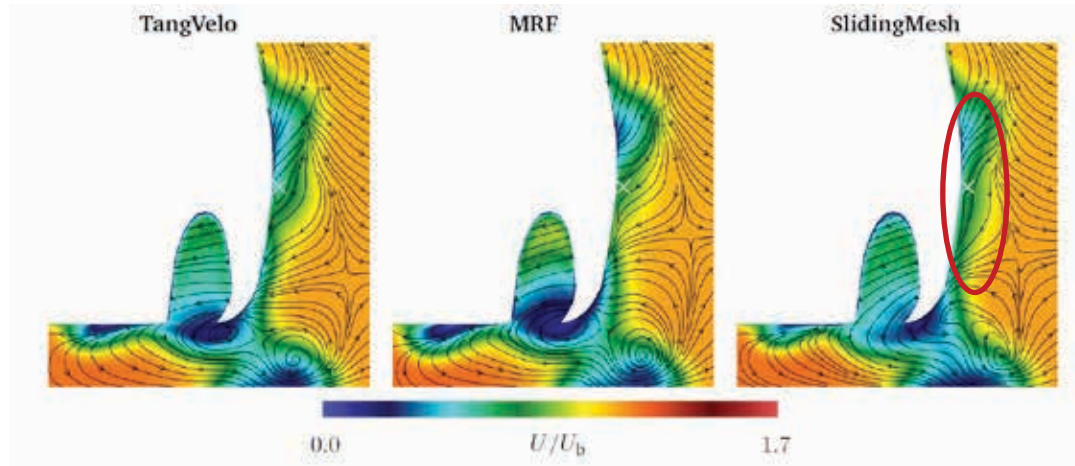
MRF



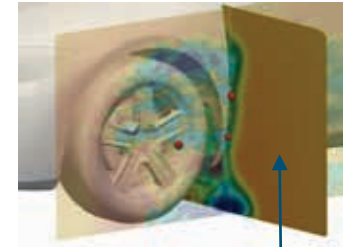
SlidingMesh



Velocity field in the wheel wake



Velocity field in the wheel wake ($ER-\zeta-f$ model)

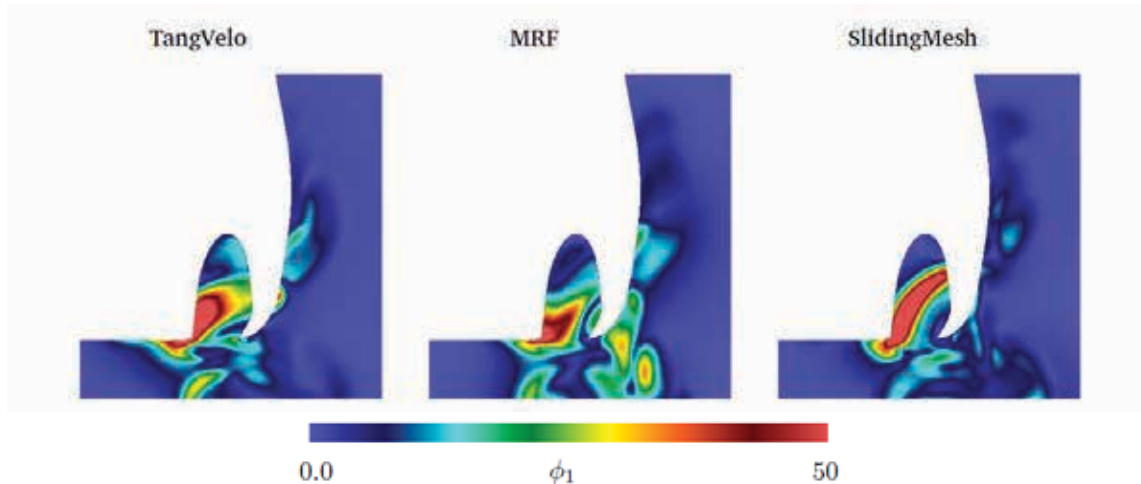


Plane

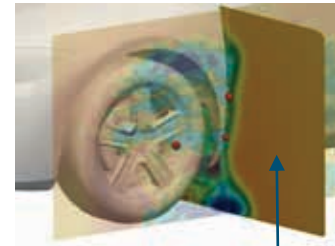
- Similar structures in the velocity field for all three wheel rotation models
- SlidingMesh velocity profile extends further in the z-direction & moves closer to the sidewall

Proper-Orthogonal-Decomposition (POD)

- Vortex structures create a spatial and temporal correlation between locations
- POD: spatial modes and their time dynamic
 - isolated view of vortex structures sorted by their turbulent kinetic energy fraction

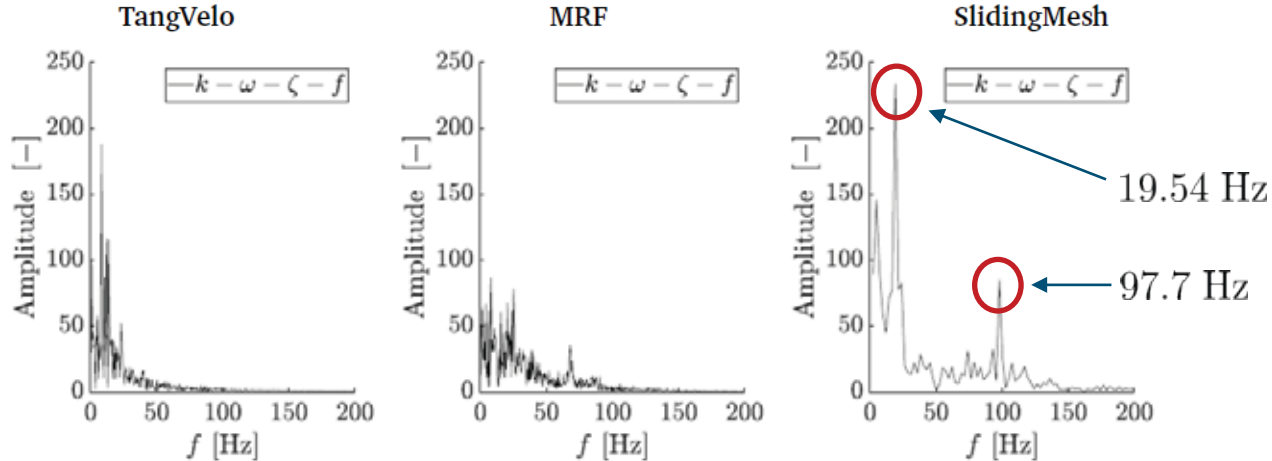


First POD mode in the wheel wake ($ER-\zeta-f$ model)



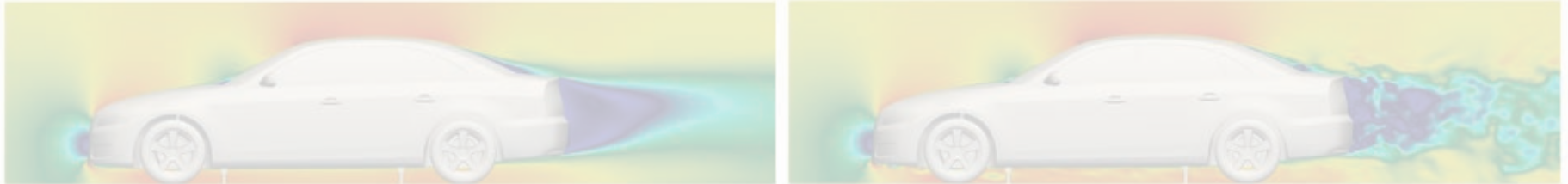
Plane

Proper-Orthogonal-Decomposition (POD)

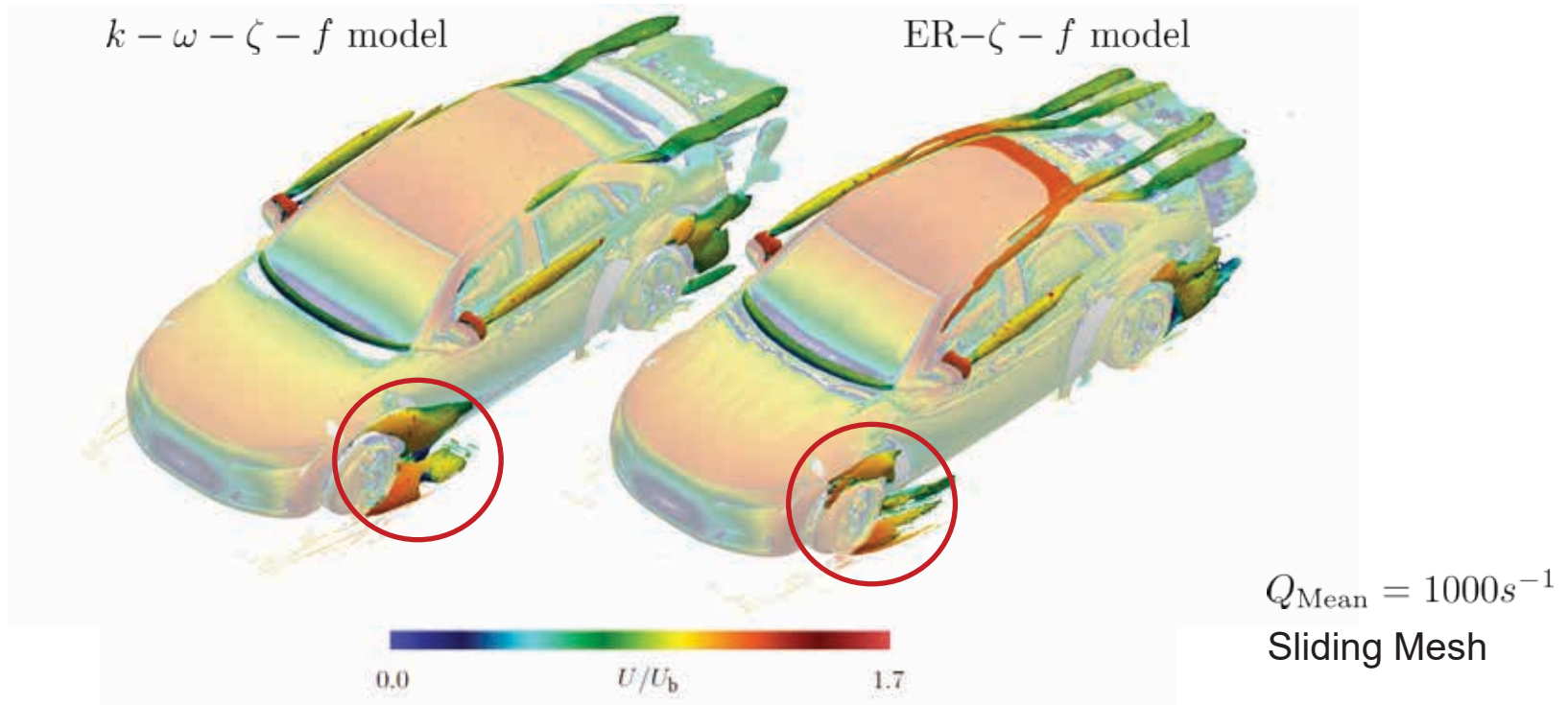


- Dominating frequency corresponds to the frequency of one complete wheel revolution ($f = 19$ Hz)
- TangVelo/ MRF frequency spectra differ significantly from SlidingMesh result

What is the influence of the turbulence model?



Characteristic vortex structures



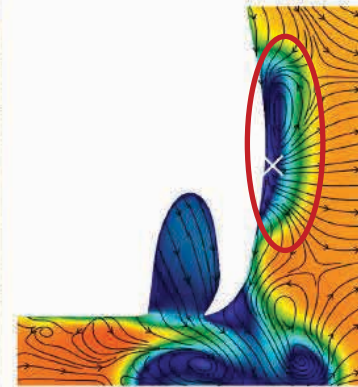
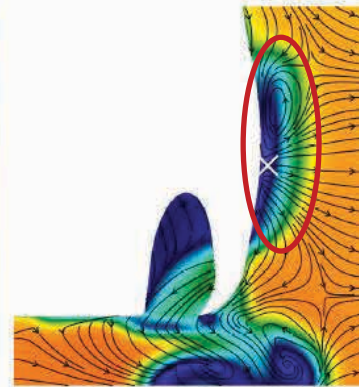
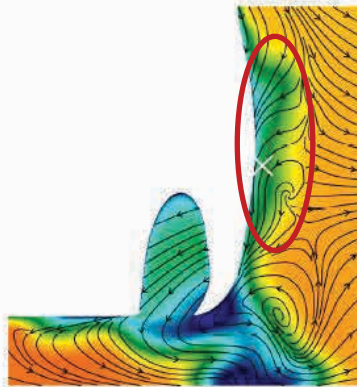
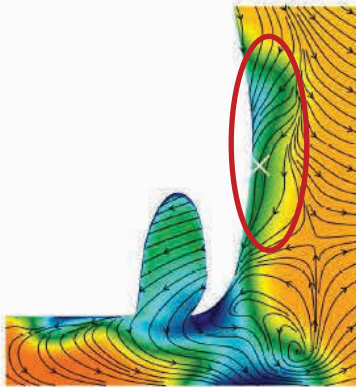
Velocity field in the wheel wake

HYBRID

RANS/URANS

ER - ζ - f

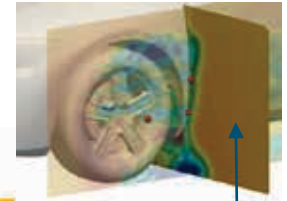
DDES - SA

 k - ω - ζ - f k - ω - SST

0.0

 U/U_b

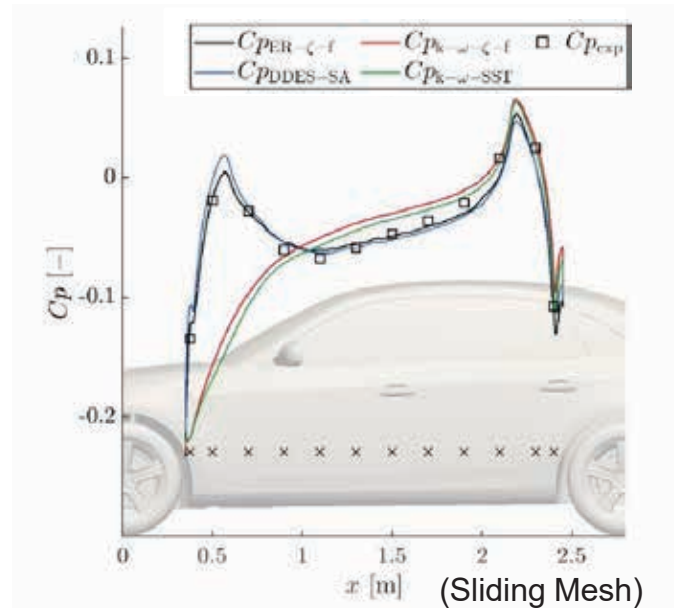
1.7



Plane

Velocity field in the wheel wake at location P2 (Sliding Mesh)

Pressure coefficient along the vehicle side



Wheel wake only correctly captured by scale-resolving turbulence models

subject 1

Research Association of Automotive Technology (FAT)

FKFS wind tunnel



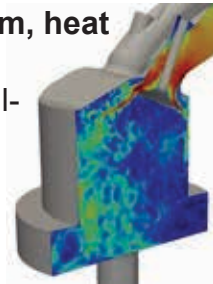
Numerical simulation



subject 2

German Research Foundation (DFG)

→ **Development of a modeling basis for the computational capturing of the simultaneous turbulent momentum, heat and mass transfer processes** of developing free shear as well as wall-boundary layers.



→ **Dynamic movement of the rim geometry**

- Transient phenomena due to rim rotation

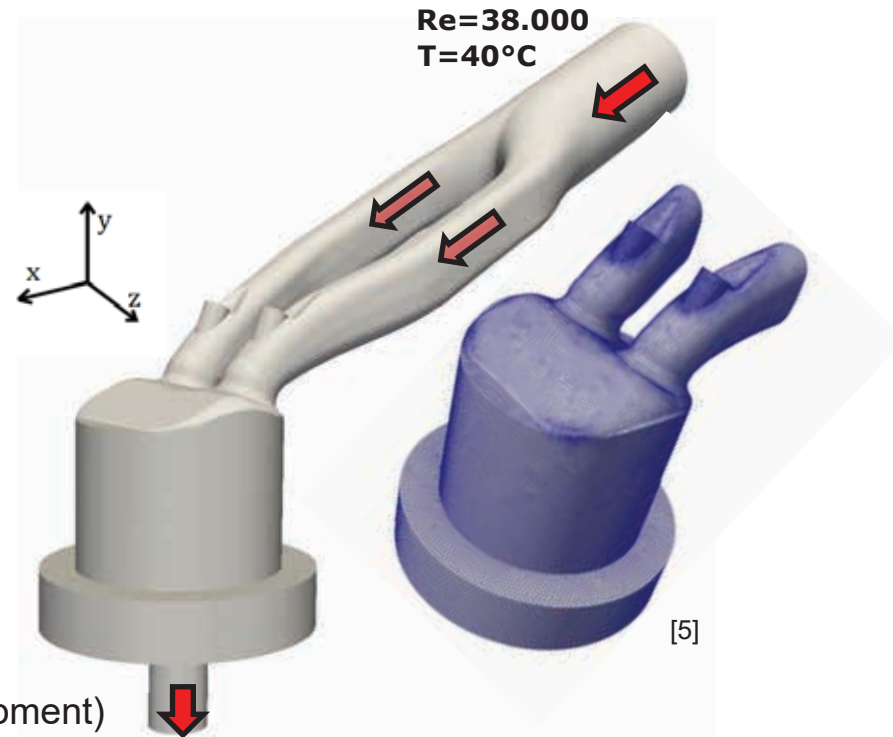
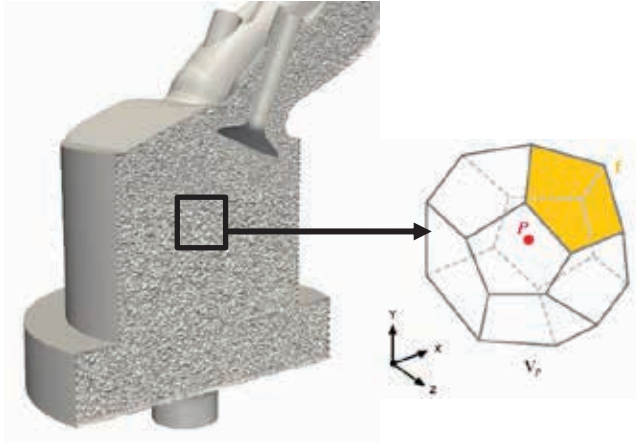
→ **Hybrid RANS/LES turbulence models**

- Flow fields including turbulent fluctuations

High requirements for the mesh quality → ANSA

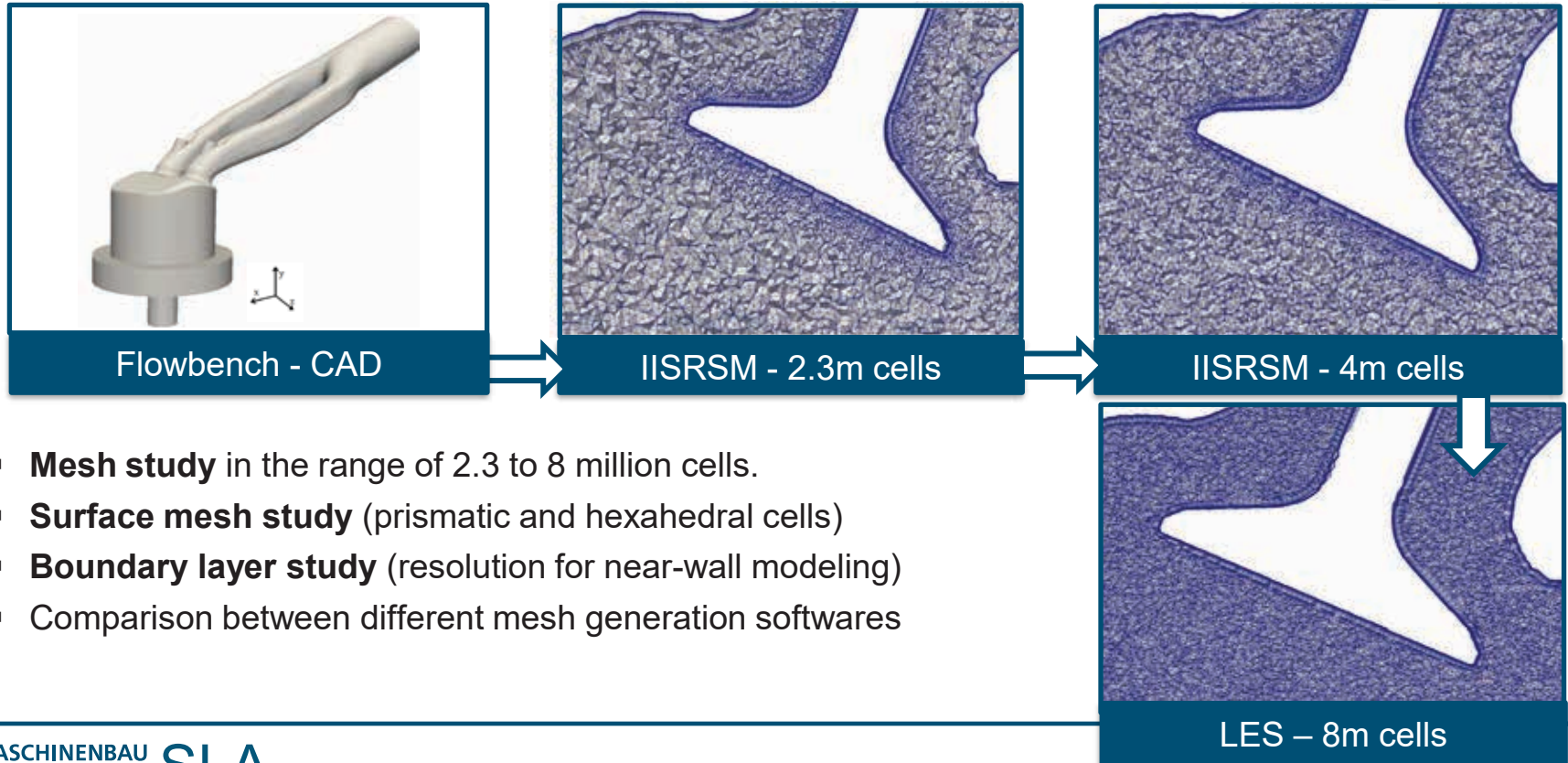
IC-Engine Intake Flow, Flowbench

- **Geometry** → CA = 270° bTDC
- **Meshing software** → ANSA pre-processor



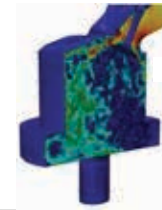
- **Simulation software** → OpenFOAM
 - Eddy-resolving RANS-RSM model (own development)

Mesh study

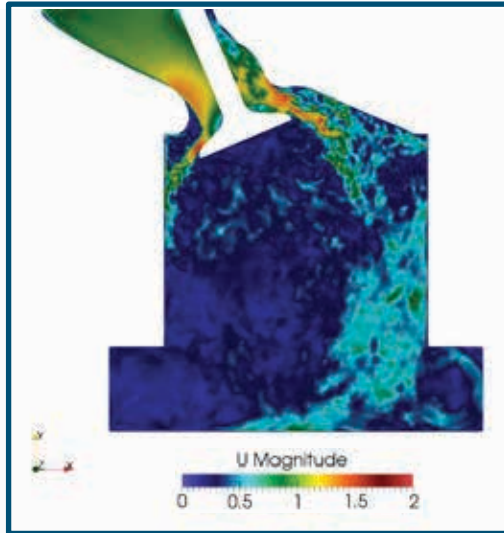


- **Mesh study** in the range of 2.3 to 8 million cells.
- **Surface mesh study** (prismatic and hexahedral cells)
- **Boundary layer study** (resolution for near-wall modeling)
- Comparison between different mesh generation softwares

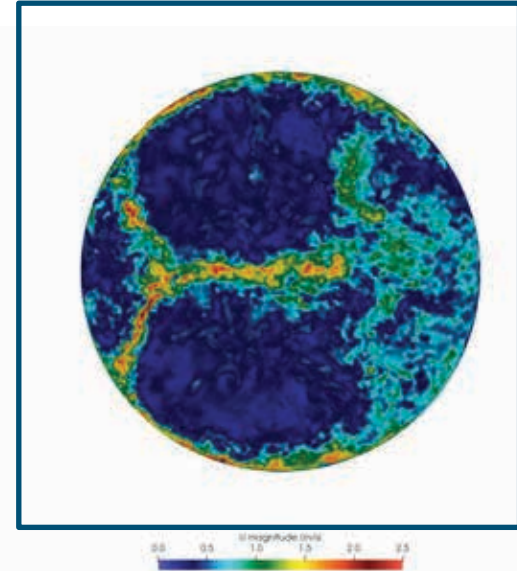
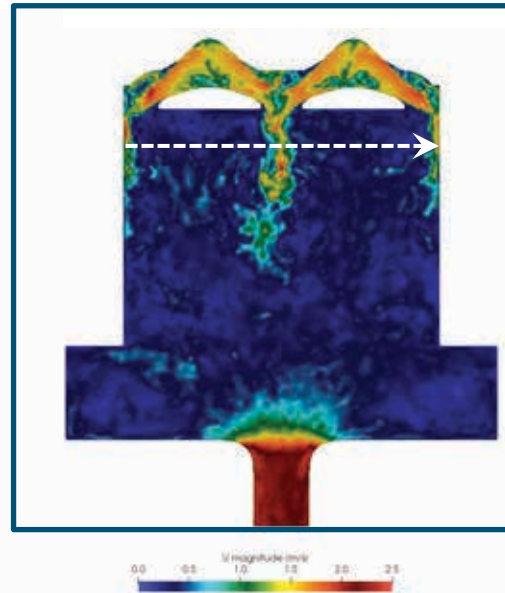
Instantaneous velocity field



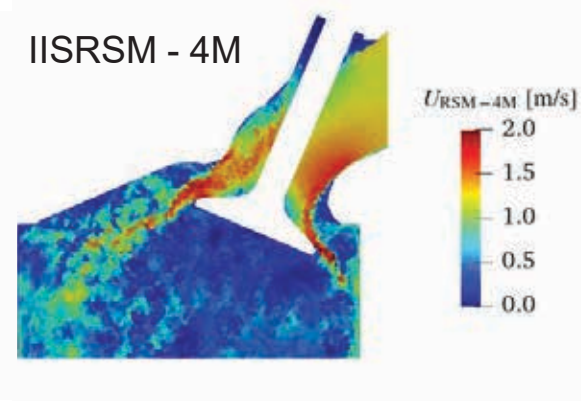
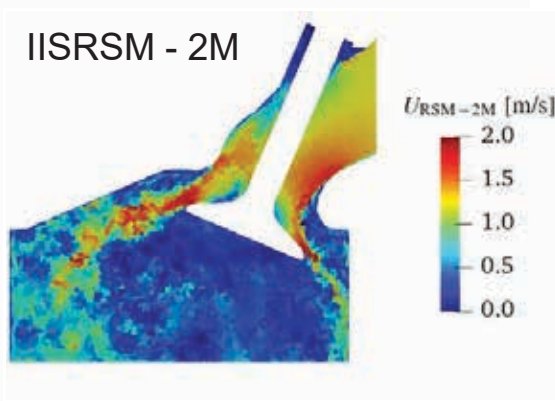
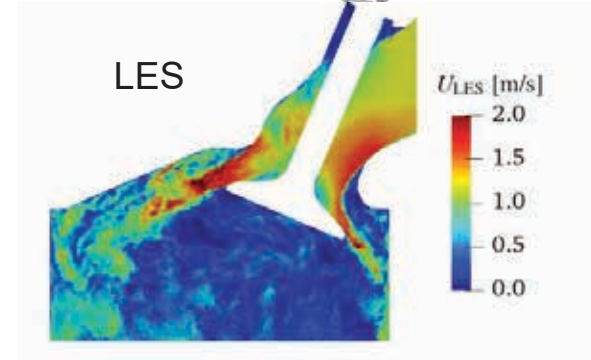
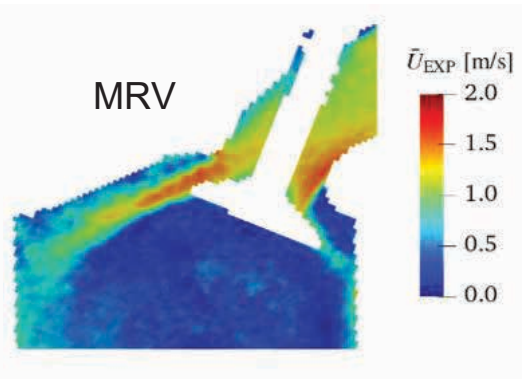
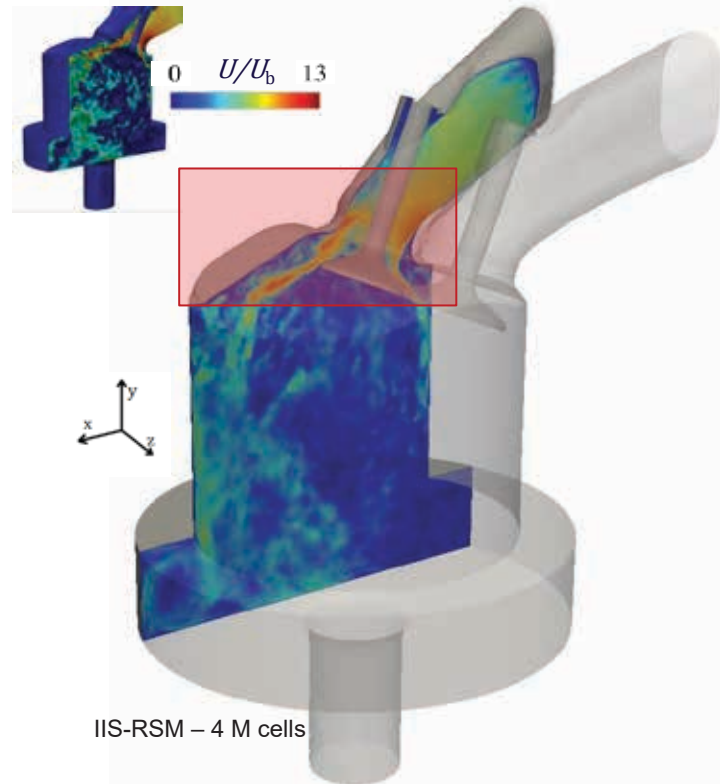
Tumble plane



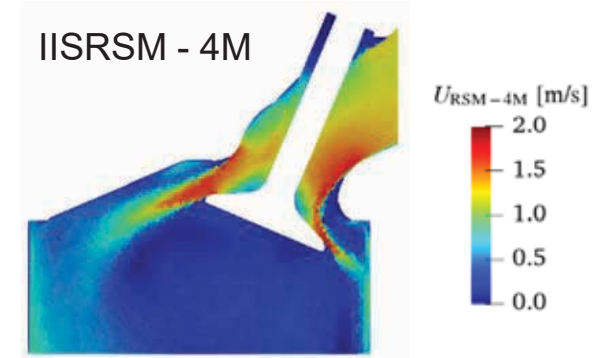
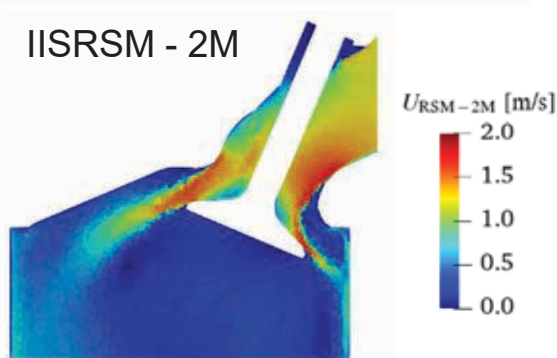
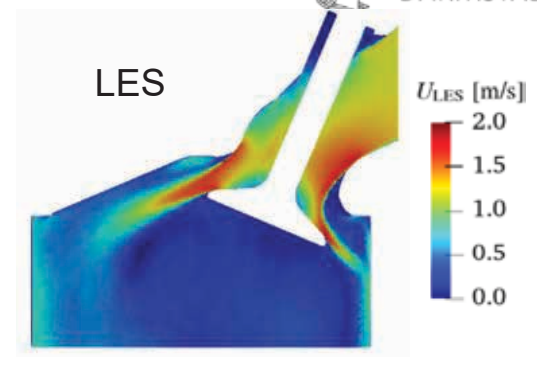
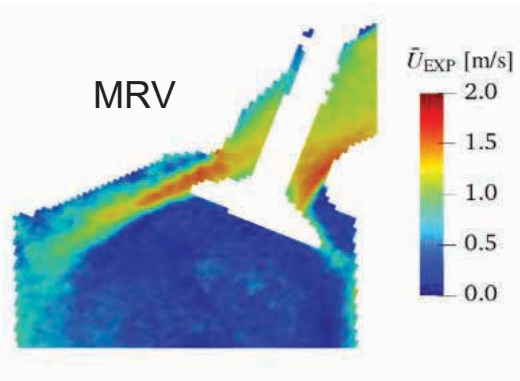
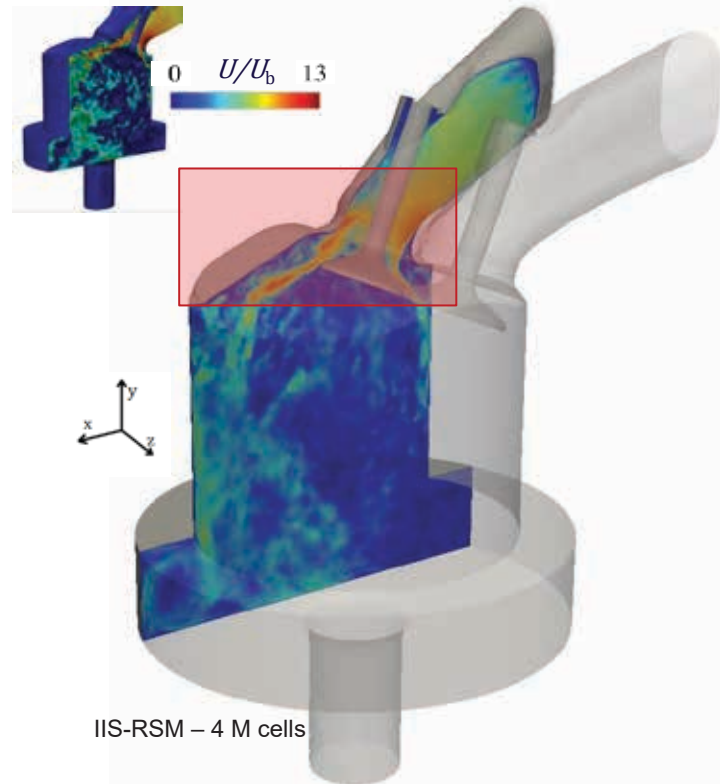
Jet collision plane



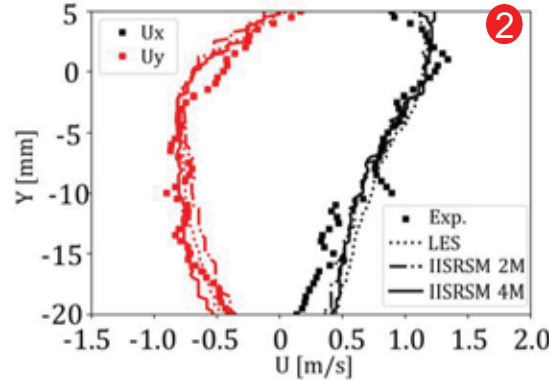
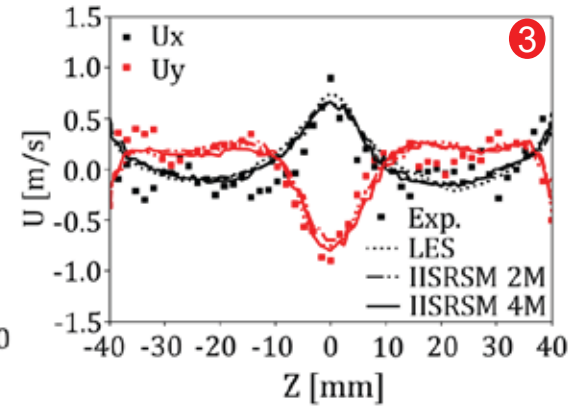
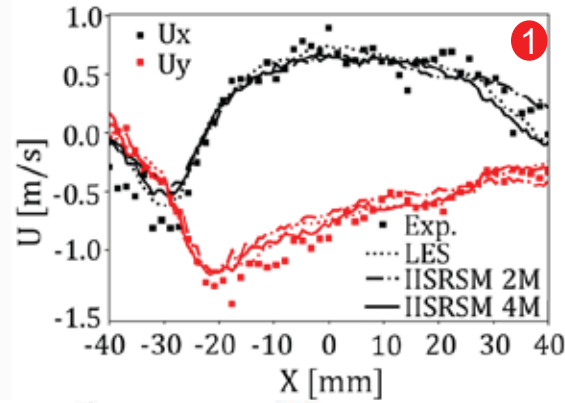
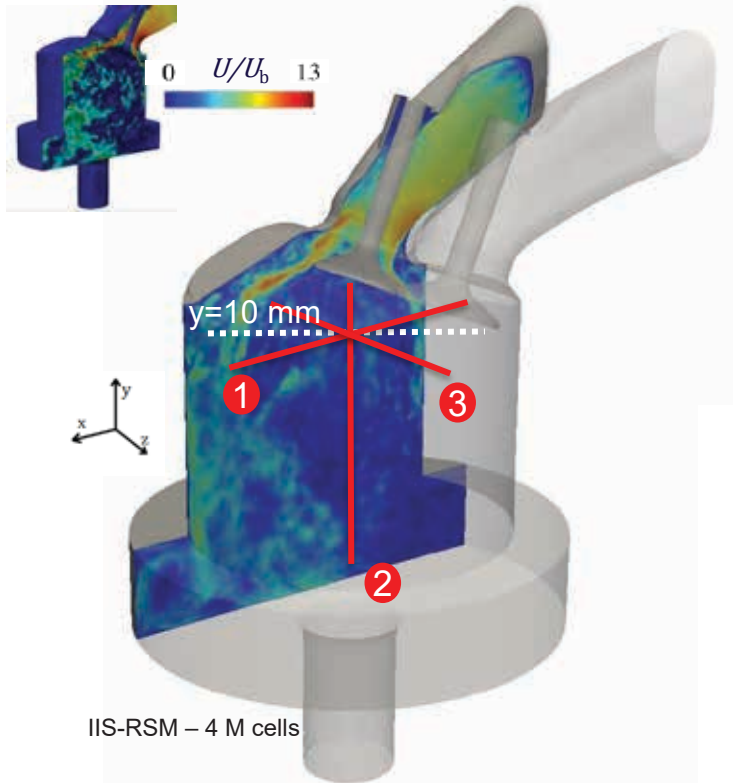
Instantaneous velocity field



Time-averaged velocity field



Time-averaged velocity field profiles



Summary

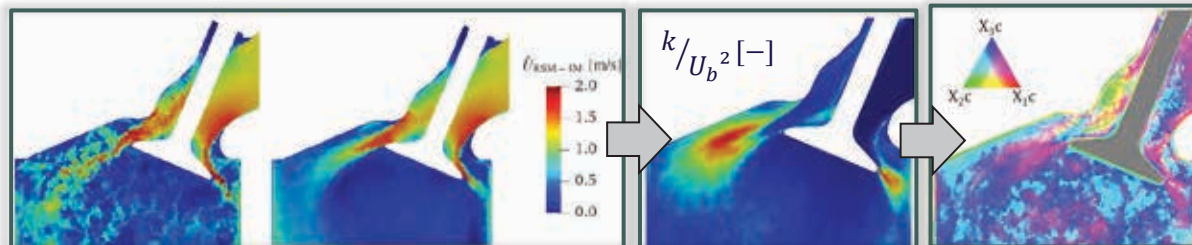
Influence of the wheel rotation approach

- Additional vortex structure + influence on local flow conditions
- Time dynamics of the velocity field + first POD mode
- Qualitative agreement of stationary & dynamic models

Influence of the turbulence model

- Wheel wake only correctly captured by scale-resolving turbulence models

Comparative evaluation of mean velocity and turbulent quantities → anisotropy characterization



References

- [1] – Johannes Burgbacher. 68. Arbeitskreissitzung FAT AK6, Handout (2022)
- [2] – John Hart. „Comparison of Turbulence Modeling Approaches to the Simulation of a Dimpled Sphere“. In: *Procedia Engineering* 147 (2016). S. 68–73.
- [3] – https://mdolab-mach-aero.readthedocs-hosted.com/en/latest/_images/overset_guide_4.jpg
- [4] – Oliver T. Schmidt. “Guide to Spectral Proper Orthogonal Decomposition”. In: *American Institute of Aeronautics and Astronautics* (2020)
- [5] - Freudenhammer, D., Baum, E., Peterson, B., Böhm, B. & Grundmann, S., “Towards time-resolved magnetic resonance velocimetry for IC-engine intake flows mag.” EXiF 55, 2015



BACKUP

Computational framework

Eddy-resolving $k - \omega - \zeta - f$ model

 $k - \omega - \zeta - f$ model

$$\left(\frac{D\omega}{Dt}\right)_{k-\omega-\zeta-f} + P_{SAS} = \left(\frac{D\omega}{Dt}\right)_{ER-\zeta-f}$$

 ER- $\zeta - f$ model

$$\left(\frac{D\omega}{Dt}\right)_{ER-\zeta-f} = C_{\omega 1} \frac{\omega}{k} P_k - C_{\omega 2} \omega^2 + \frac{\partial}{\partial x_i} \left[\left(\nu + \frac{\nu_t}{\sigma} \right) \frac{\partial \omega}{\partial x_i} \right] + CD + P_{SAS}$$

P_{SAS} formulated directly in terms of the second derivative of the velocity field instead of von Karman length scale (following Maduta *et al.*, 2015)

$$P_{SAS} = C_{SAS} \max \left(\sqrt{\frac{\partial^2 \bar{U}_i}{\partial x_j \partial x_j} \frac{\partial^2 \bar{U}_i}{\partial x_k \partial x_k}} \sqrt{k} - C_{T_2} T_2, 0 \right)$$

The model doesn't explicitly include a grid-dependent parameter:
 ⇒ towards a grid-spacing-free model formulation

Turbulence model: Eddy-resolving URANS-RSM → IIS-RSM**

$$\frac{\partial}{\partial t}(\overline{U}_i) + \overline{U}_j \frac{\partial(\overline{U}_i)}{\partial x_j} = \frac{\partial}{\partial x_j} \left[\nu \left(\frac{\partial \overline{U}_i}{\partial x_j} \right) - \overline{u'_i u'_j} \right]$$

- ▶ Sensitized RANS momentum equation
→ instantaneous velocity field

$$\frac{D\overline{u'_i u'_j}}{Dt} = P_{ij} + \Phi_{ij} - \epsilon_{ij}^h + (0.5D_{ij}^\nu + D_{ij}^{\rho'} + D_{ij}^{u'})$$

- ▶ Transport equation for sub-scale stress tensor

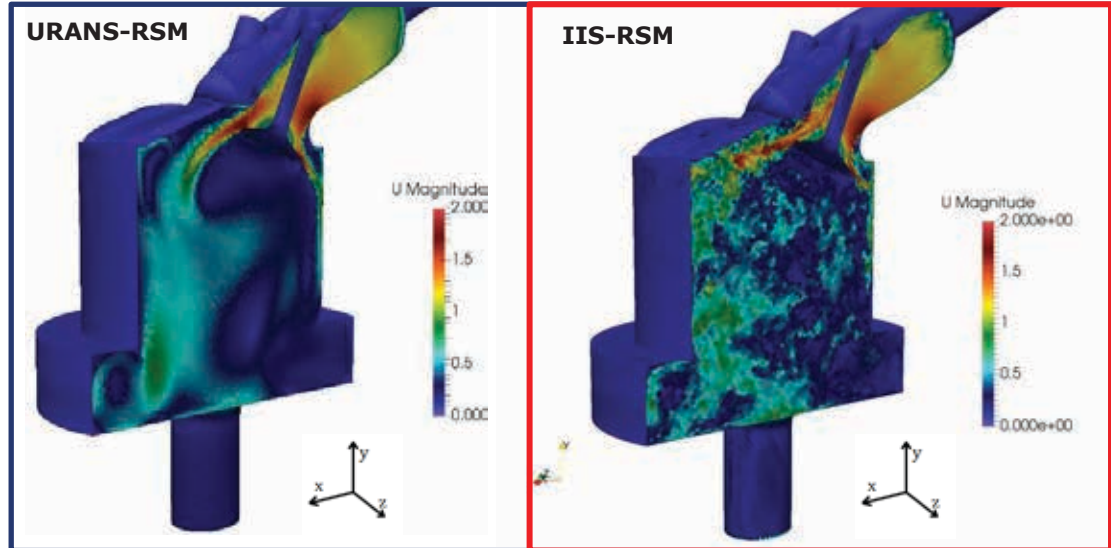
$$\epsilon_{ij}^h = f_s \overline{u_i u_j} \frac{\epsilon_h}{k} + (1 - f_s) \frac{2}{3} \epsilon_h \delta_{ij}$$

- ▶ Model extension toward an eddy-resolving version (SAS*-related)

$$\left(\frac{D\omega^h}{Dt} \right)_{IIS-RSM} = \left(\frac{D\omega^h}{Dt} \right)_{RSM} + P_{IIS-RSM}$$

$$\epsilon_h = \omega_h k$$

$$P_{IIS-RSM} = f(\nabla^2 U_i)$$



Computational framework

Eddy-resolving $k - \omega - \zeta - f$ model

- Ensemble-averaged continuity and momentum equations for incompressible Newtonian fluids

$$\frac{\partial \bar{U}_i}{\partial x_i} = 0 \quad \frac{\partial \bar{U}_i}{\partial t} + \bar{U}_j \frac{\partial \bar{U}_i}{\partial x_j} = -\frac{1}{\rho} \frac{\partial \bar{p}}{\partial x_i} + \frac{\partial}{\partial x_j} \left(\nu \frac{\partial \bar{U}_i}{\partial x_j} - \underbrace{\overline{u_i u_j}}_{\text{RST}} \right)$$

- Boussinesq eddy-viscosity hypothesis for Reynolds stress tensor modeling

$$\overline{u_i u_j} = -2\nu_t \bar{S}_{ij} + \frac{2}{3} k \delta_{ij} \quad \bar{S}_{ij} = \frac{1}{2} \left(\frac{\partial \bar{U}_i}{\partial x_j} + \frac{\partial \bar{U}_j}{\partial x_i} \right)$$

$$\nu_t = C_\mu^* \zeta k T$$

$k - \omega - \zeta - f$ model

ER- $\zeta - f$ model

Characteristic vortex structure

Sliding Mesh

$k - \omega - \zeta - f$ model



ER- $\zeta - f$ model



0.0

U/U_b

1.7

$$\text{FlowType} = -0.1$$

$$\text{FlowType} = \frac{|S| - |\Omega|}{|S| + |\Omega|}$$